

CS151 Intro to Data Structures

Iterators

Recursion

Binary Search

Announcements

- HW03 due tomorrow
- Lab 4 and 5 due dates?
 - Lab 4 was interfaces. Due tomorrow...
 - Lab 5 was stacks. Related to your homework but due next thursday?
 - Next two labs will not be checked off. They're just a head start on your homework.

Outline

- Iterators
- Runtime
- Recursion
- Binary Search

ArrayList ADT

Whats an ADT?

ArrayList

Big-O memory?

- $O(n)$

Indexing / random access?

- $O(1)$

Add / remove?

- $O(n)$

Iterators

Iterators

- represents a sequence of elements and provides a way to iterate, or traverse, through those elements one at a time

Iterators

- Abstracts the process of scanning through a sequence of elements (traversal)
- provides a way to iterate, or traverse, through elements one at a time

`hasNext()`: Returns true if there is at least one additional element in the sequence, and false otherwise.

`next()`: Returns the next element in the sequence.

- Combination of these two methods allow a generic traversal structure

```
while (iter.hasNext ()) {  
    iter.next ();  
}
```


Iterators

- **code**
- Can an iterator go backwards? NO. Only can do `next()`

Iterable Interface

- What can i use an `iterator` on? Anything that implements the `iterable` interface.
- Each call to `iterator()` returns a new iterator instance, thereby allowing traversals of a collection
- `List` interface extends `Iterable` and `ArrayList` implements `List`

Iterable Interface

An interface with a single method:

- `iterator()`: returns an iterator of the elements in the collection

Iteratoror Interface

Iterator or Interface

Another interface that supports iteration

- `boolean hasNext()`
- `E next()`
- `void remove()`

- `Scanner` implements `Iterator<String>`
- `ArrayList` inner class `ArrayListIterator` implements `Iterator`

Let's make ExpandableArray iterable

Iterable versus Iterator?

- Iterable

- `java.lang`
- **override** `iterator()`
- Doesn't store the iteration state
- Removing elements during iteration isn't allowed

- Iterator

- `java.util`
- **Override** `hasNext()`, `next()`
- **Optional** `remove()`
- Stores iteration state (list cursor)
- Removing elements during iteration supported

Iterators Review

Iterators

- represents a sequence of elements and provides a way to iterate, or traverse, through those elements one at a time

Iterators

- Abstracts the process of scanning through a sequence of elements (traversal)
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while (iter.hasNext()) {  
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}
```

Iterators

Can an iterator go backwards? NO. Only can do `next ()`

Iterable Interface

An interface with a single method:

- `iterator()`: returns an iterator of the elements in the collection

Iterator Interface

Another interface that supports iteration

- `boolean hasNext()`
- `E next()`
- `void remove()`

- `Scanner` implements `Iterator<String>`
- `ArrayList` **inner class** `ArrayListIterator` implements `Iterator`

Iterable Expandable Array

Iterable versus Iterator?

- Iterable

- `java.lang`
- **override** `iterator()`
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- Iterator

- `java.util`
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- Stores iteration state (list cursor)
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Runtime Analysis Review

Data Structure Operation Runtime

	Array	ArrayList	Linked list	ArrayStack	ArrayQueue
random access					
insert					
remove					
search					
min/max					

Dynamic Array

Array is replaced with a larger one when `add` is performed on full

- Allocate a new larger array
- Copy all existing elements into the beginning of new array

How much bigger?

- incremental: increase size by a constant c
- doubling: double the size

Amortized Analysis

The worst case is unlikely to occur

Amortized: the average run time over a series of operations

Accounts for an uneven distribution of work

Amortized Analysis of an Expandable Array

When the array is full, we can have two expansion strategies

- expand the array by doubling the size
 - `new_arr[numElems*2]`
 - “doubling expansion”
- expand the array by a constant c
 - `new_arr[numElems+c]`
 - “incremental expansion”

Amortized Analysis of “Doubling Expansion”

Example: start with an array of size 1

Let’s compute two things:

1. the number of times we need to expand: $k(n)$
2. the total number operations: $T(n)$

$$k(8) = 3$$

$$\mathbf{k(n) = \log n}$$

$$T(8) = 1 + 2 + 3 + 1 + 5 + 1 + 1 + 1 = 15$$

$$\mathbf{T(n) = n}$$
 (as n approaches infinity)

Amortized $T(n)$?

$$O(n) / n = O(1)$$

Amortized Analysis of “Incremental Expansion”

Example: start with an array of size 1 and expand with $c=2$

Let's compute two things:

1. the number of times we need to expand: $k(n, c)$
2. the total number operations: $T(n)$

$$k(6, 2) = 3$$

$$\mathbf{k(n, c) = n/c}$$

$$T(6) = 1 + 2 + 1 + 4 + 1 + 6 = 15$$

$$\mathbf{T(n) = O(n^2)} \text{ (as } n \text{ approaches infinity)}$$

Amortized $T(n)$?

$$\mathbf{O(n^2) / n = O(n)}$$

Outline

- Runtime
- **Recursion**
- Binary Search

Recursive functions – base case

Conditional statement that prevents infinite repetitions

Usually handles cases where:

- input is empty

- problem is at its smallest size

Recursion Example - Factorial

- What is a factorial? $n!$
- product of all integers less than or equal to n
 - $n! = n * n-1 * n-2 \dots 1$
 - $5! = 5 * 4 * 3 * 2 * 1$
 - $4! = 4 * 3 * 2 * 1$
 - $3! = 3 * 2 * 1$

Visualizing recursion – Factorial example

factorial(5) =

= 5 * factorial(4)

= 5 * 4 * factorial(3)

= 5 * 4 * 3 * factorial(2)

= 5 * 4 * 3 * 2 * factorial(1)

= 5 * 4 * 3 * 2 * 1

Recursion Example – Contains letter

Write a method called “containsLetter” that determines if a String contains a given character

Question: What are the parameters?

1. The character to look for
2. The string to be looking in

Question: What is the return type?

Code it!

Recursion Visualization – Contains letter

```
contains("l", "apple") =  
  contains("l", "apple")  
    contains("l", "pple")  
      contains("l", "ple")  
        contains("l", "le")  
          return true
```

Recursive Method

Break problem down into smaller subproblem that we can repeat

Base case(s):

- no recursive calls are performed
- every chain of recursive calls must reach a base case eventually

Recursive calls:

- Calls to the same method in a way that progress is made towards a base case
- Often called “the rule”

Compiled Code

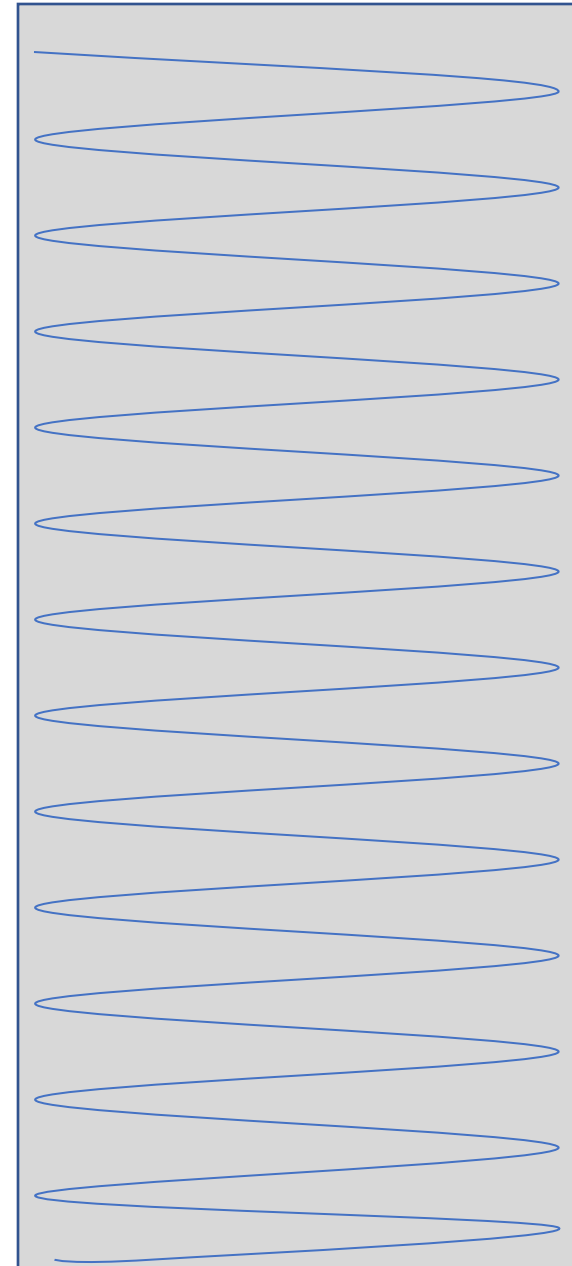
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2.     int A = 10;  
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1. int factorial(int n) {  
2.     if (n == 1) {  
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5.         int F = n *  
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```

Executing Function



Call Stack




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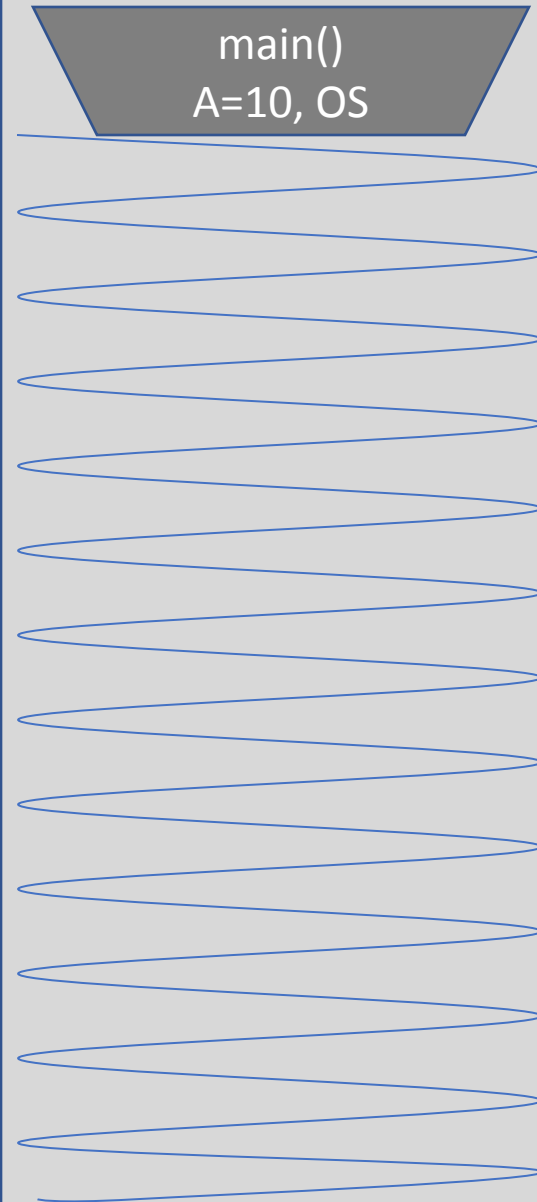
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Executing Function



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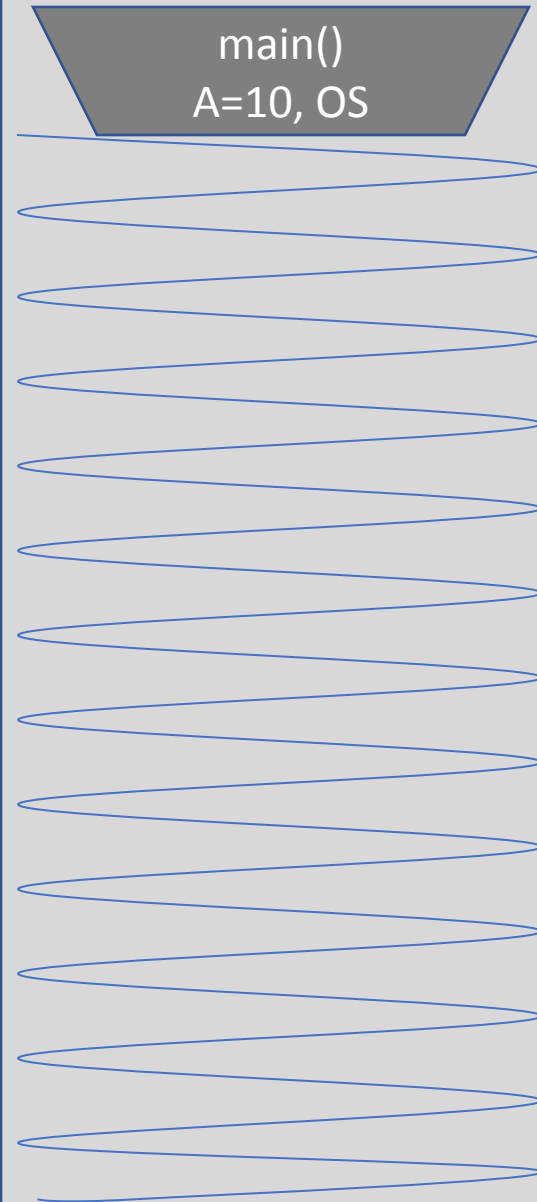
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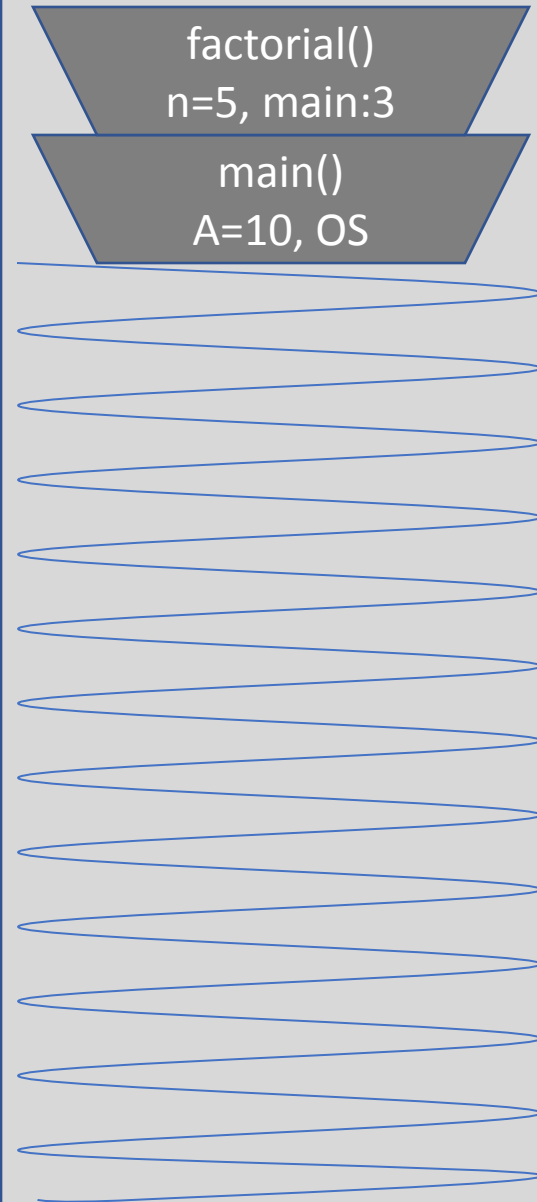
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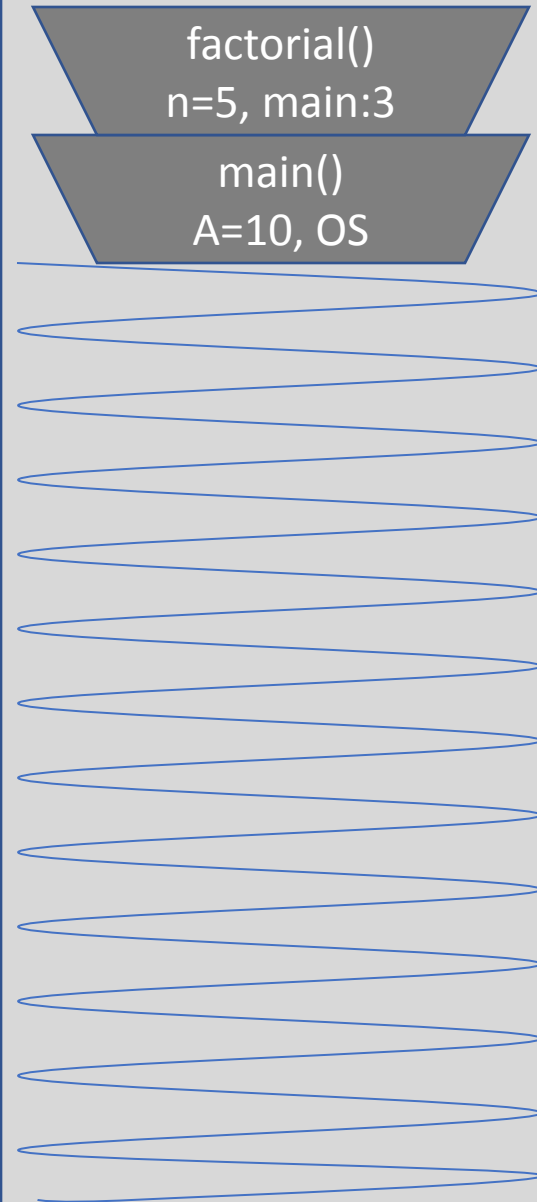
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Executing Function

```
int factorial(int n=5) {  
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4.     } else {  
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Call Stack




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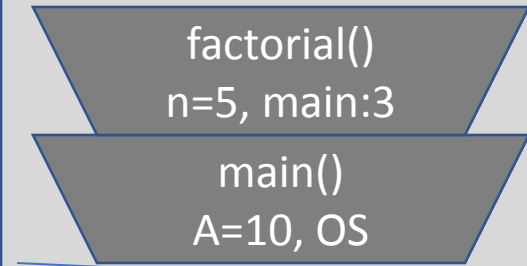
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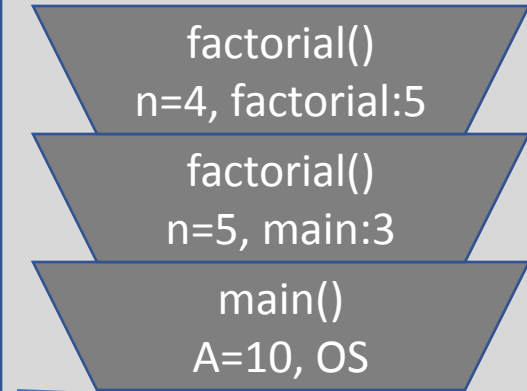
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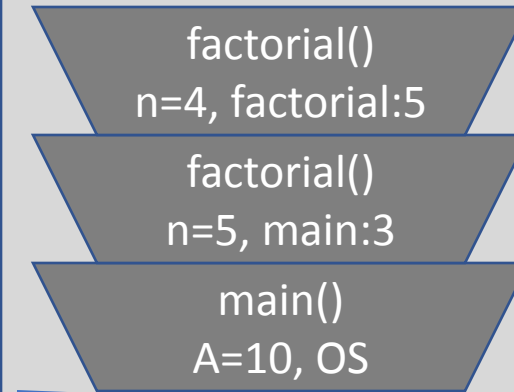
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6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```

Executing Function



```
1. int factorial(int n=4) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n *  
6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```

Call Stack




Compiled Code

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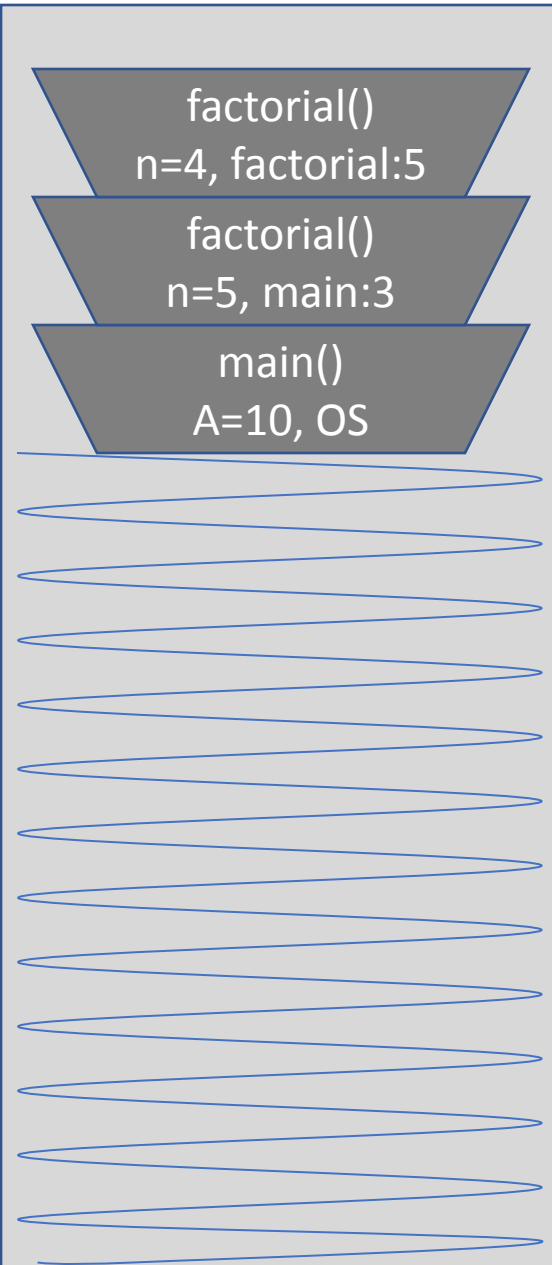
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Call Stack




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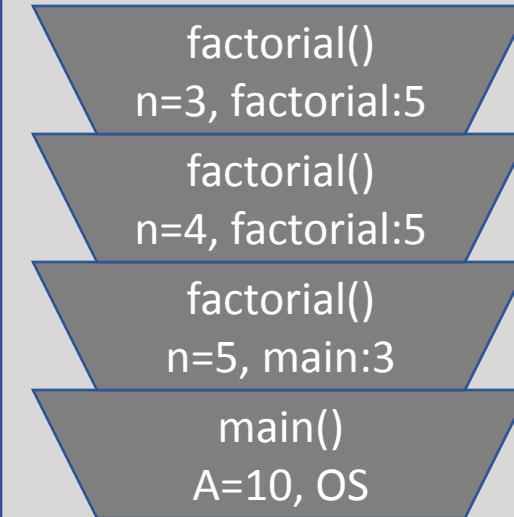
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Call Stack



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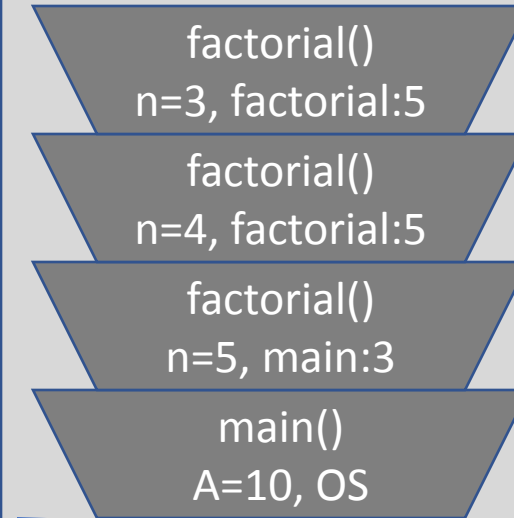
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Executing Function

```
→ 1. int factorial(int n=3) {  
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Call Stack




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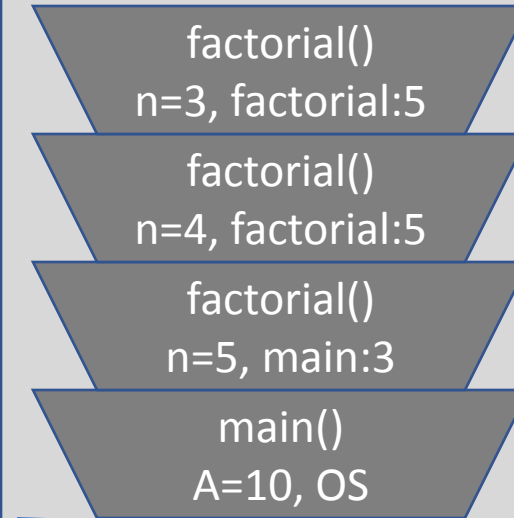
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Call Stack




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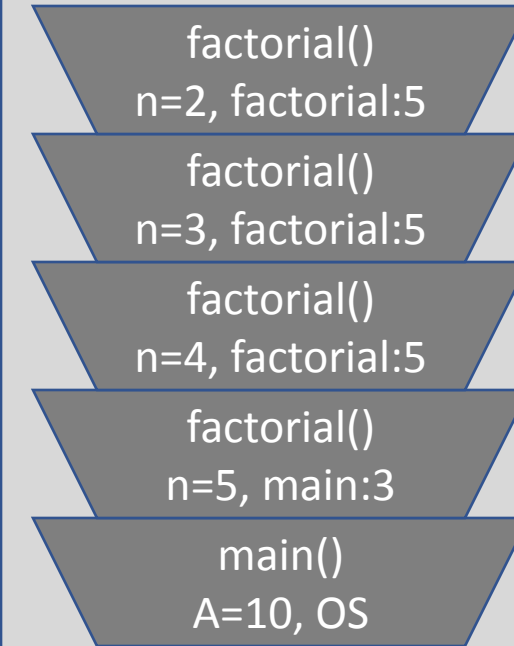
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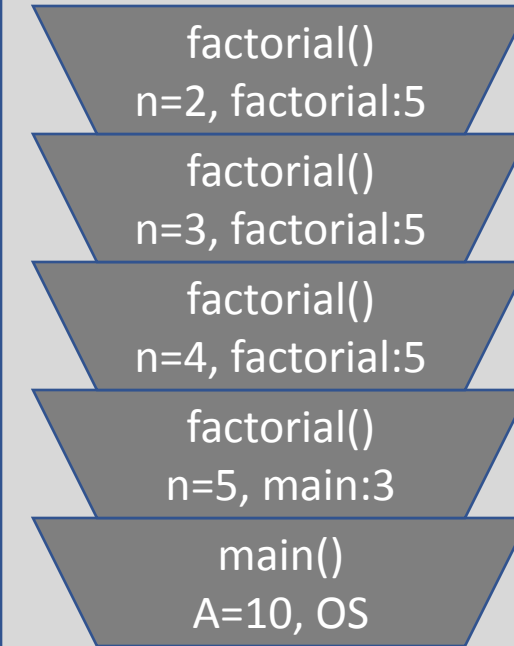
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Executing Function

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→ 1. int factorial(int n=2) {  
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4.     } else {  
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Call Stack




Compiled Code

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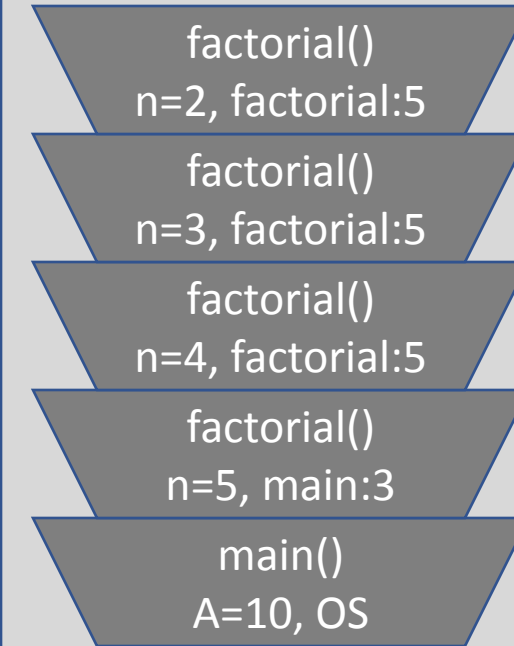
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Call Stack



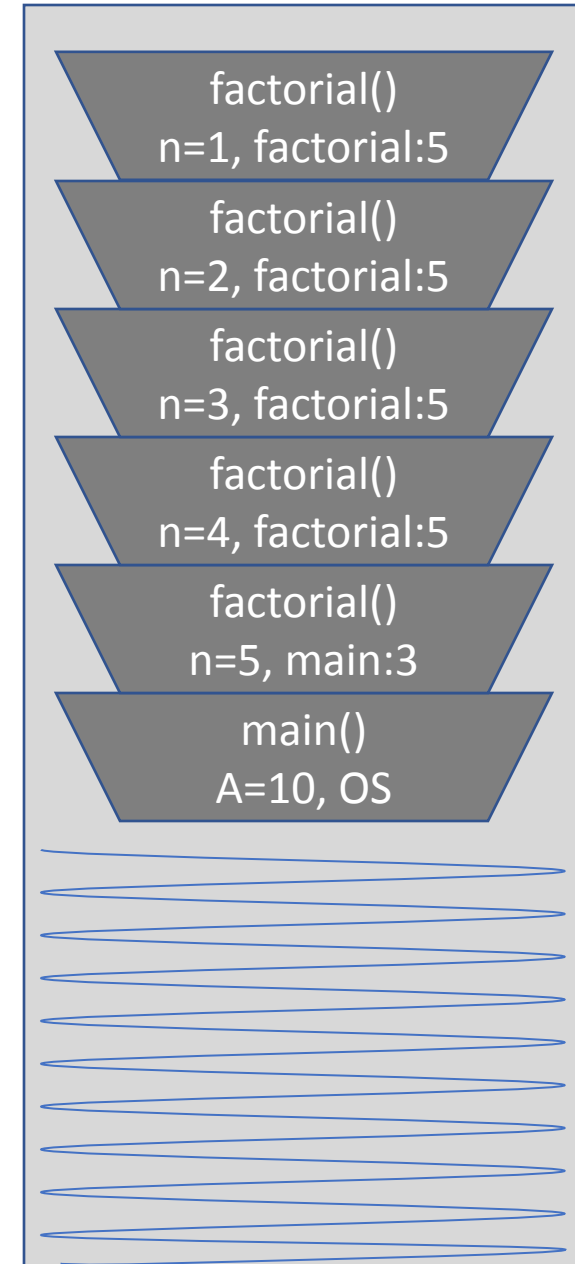

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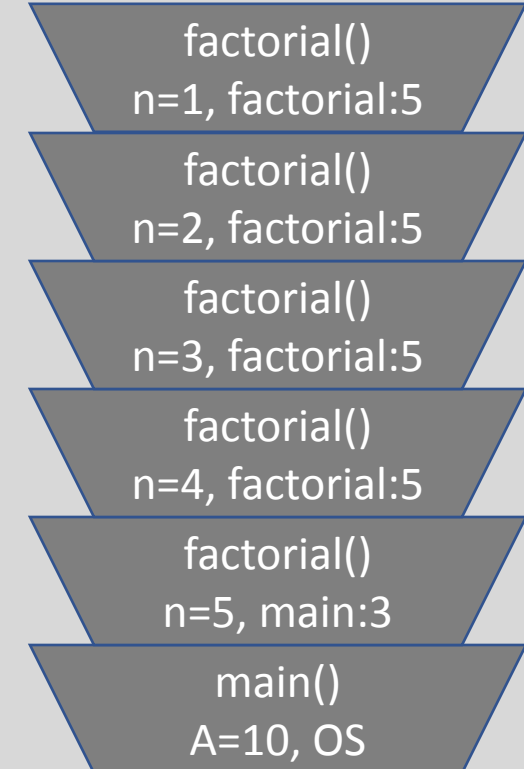
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}
```

Executing Function



```
int factorial(int n=1) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n *  
6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```

Call Stack



```
factorial()  
n=1, factorial:5  
factorial()  
n=2, factorial:5  
factorial()  
n=3, factorial:5  
factorial()  
n=4, factorial:5  
factorial()  
n=5, main:3  
main()  
A=10, OS
```


Compiled Code

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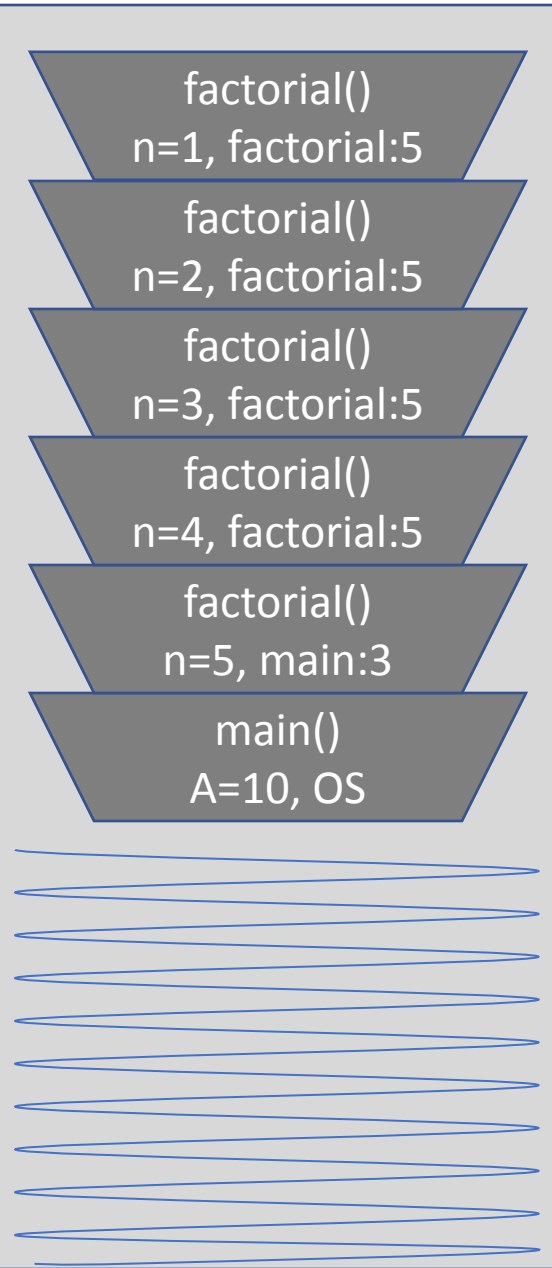
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4.     } else {  
5.         int F = n *  
6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```



Call Stack



```
factorial()  
n=1, factorial:5  
factorial()  
n=2, factorial:5  
factorial()  
n=3, factorial:5  
factorial()  
n=4, factorial:5  
factorial()  
n=5, main:3  
main()  
A=10, OS
```


Compiled Code

```
1. void main() {  
2.     int A = 10;  
3.     int B = factorial(5);  
4.     System.out.println(B);  
5. }
```

```
1. int factorial(int n) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n *  
6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```

Executing Function

```
1. int factorial(int n=2) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n * 1;  
6.         return F;  
7.     }  
8. }
```



Call Stack

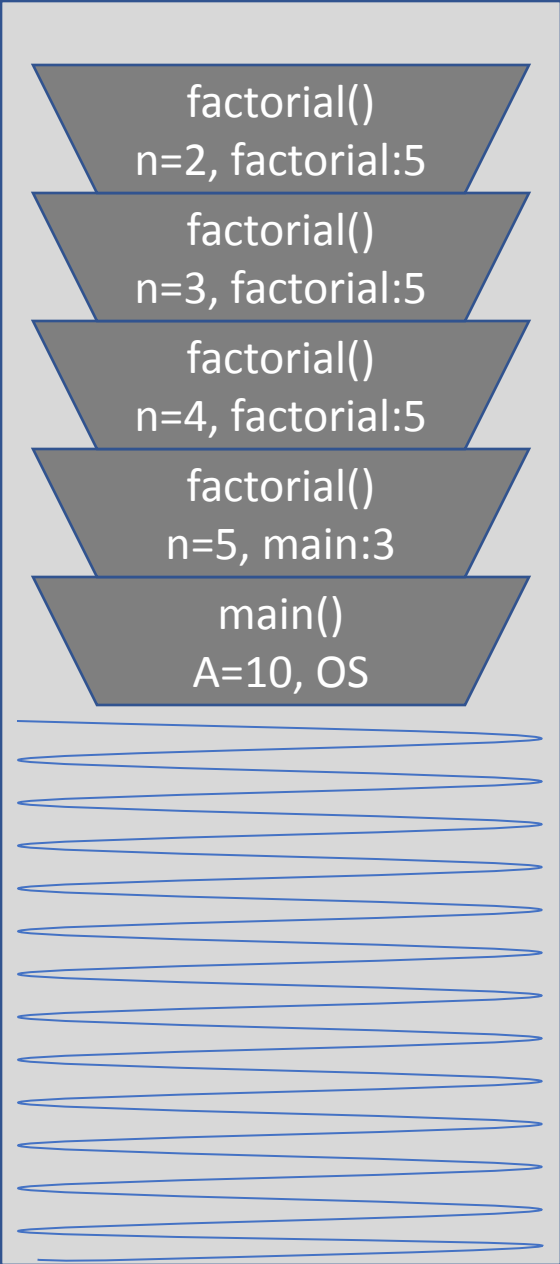
factorial()
n=2, factorial:5

factorial()
n=3, factorial:5

factorial()
n=4, factorial:5

factorial()
n=5, main:3

main()
A=10, OS




Compiled Code

```
1. void main() {  
2.     int A = 10;  
3.     int B = factorial(5);  
4.     System.out.println(B);  
5. }
```

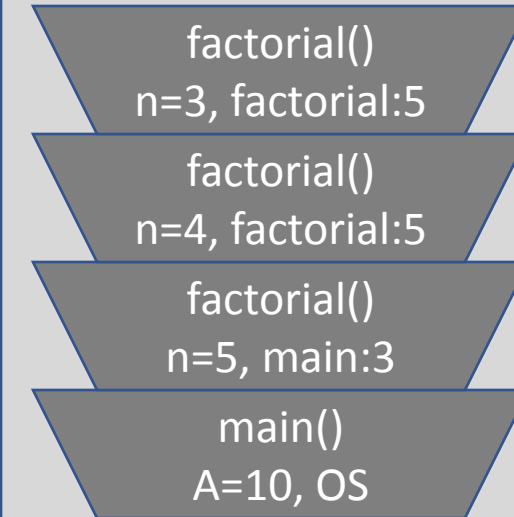
```
1. int factorial(int n) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n *  
6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```

Executing Function

```
1. int factorial(int n=3) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n * 2;  
6.         return F;  
7.     }  
8. }
```



Call Stack




Compiled Code

```
1. void main() {  
2.     int A = 10;  
3.     int B = factorial(5);  
4.     System.out.println(B);  
5. }
```

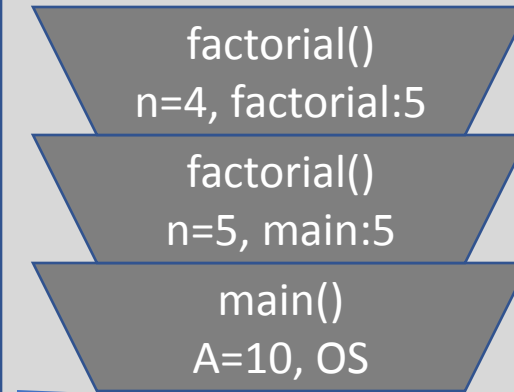
```
1. int factorial(int n) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n *  
6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```

Executing Function

```
1. int factorial(int n=4) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n * 6;  
6.         return F;  
7.     }  
8. }
```



Call Stack




Compiled Code

```
1. void main() {  
2.     int A = 10;  
3.     int B = factorial(5);  
4.     System.out.println(B);  
5. }
```

```
1. int factorial(int n) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n *  
6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```

Executing Function

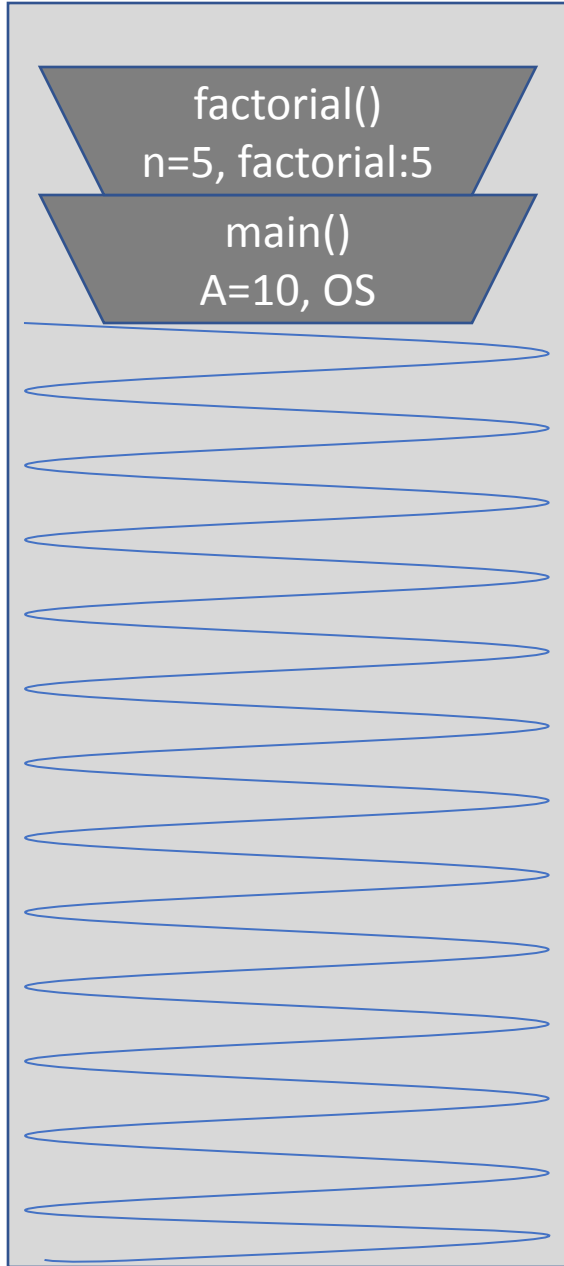
```
1. int factorial(int n=5) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n * 24;  
6.         return F;  
7.     }  
8. }
```



Call Stack

factorial()
n=5, factorial:5

main()
A=10, OS




Compiled Code

```
1. void main() {  
2.     int A = 10;  
3.     int B = factorial(5);  
4.     System.out.println(B);  
5. }
```

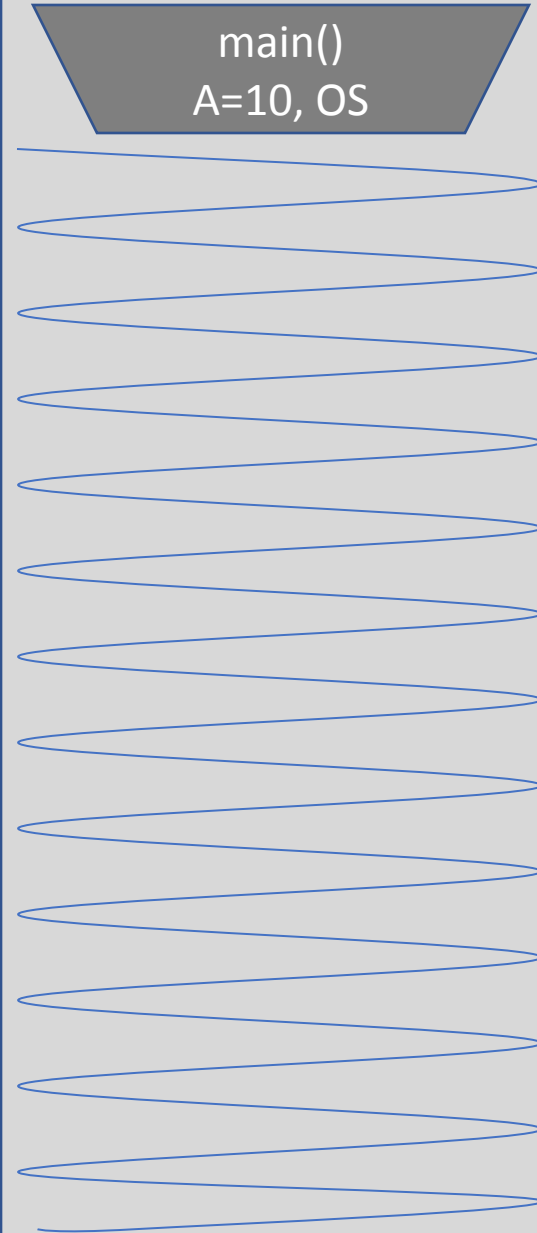
```
1. int factorial(int n) {  
2.     if (n == 1) {  
3.         return 1;  
4.     } else {  
5.         int F = n *  
6.         factorial(n-1);  
7.         return F;  
8.     }  
}
```

Executing Function

```
1. void main() {  
2.     int A = 10;  
3.     int B = 120;  
4.     System.out.println(B);  
5. }
```



Call Stack



Outline

- Runtime
- Recursion
- **Binary Search**

Binary Search

- efficient search in a sorted list
- can be implemented **recursively**

Search steps:

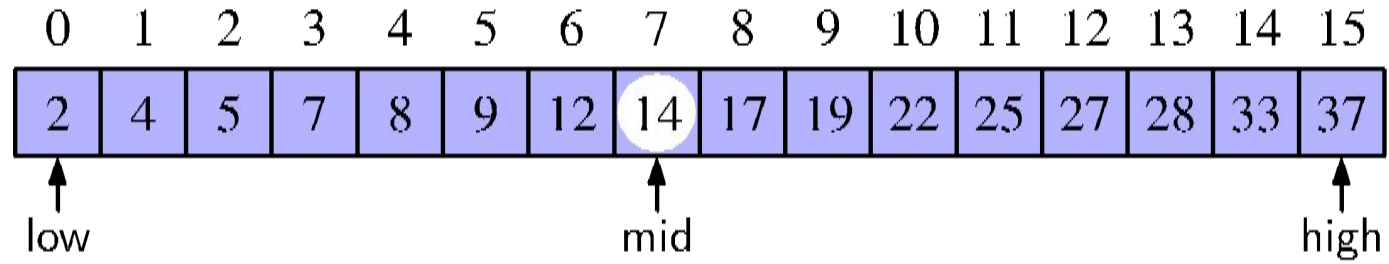
1. Calculate midpoint
2. Compare the value at the midpoint with the target value
 - a. if equal:
 - i. return index
 - b. if target value $<$ midpoint value:
 - i. **search** the left portion of the list
 - c. if target value $>$ midpoint value:
 - i. **search** the right portion of the list

Binary Search

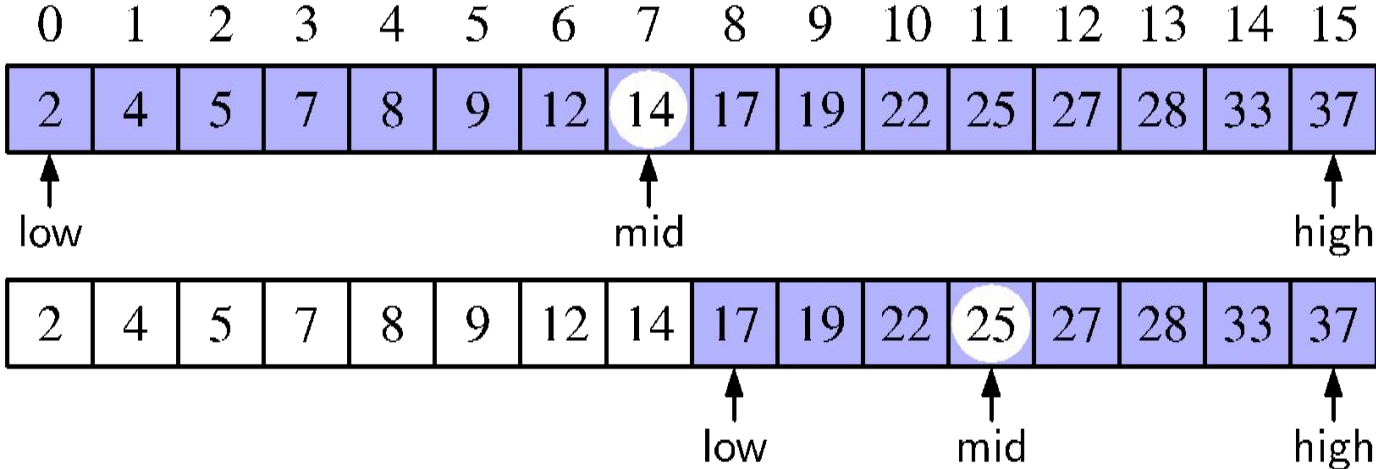
Search for an integer (22) in an ordered list

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
2	4	5	7	8	9	12	14	17	19	22	25	27	28	33	37

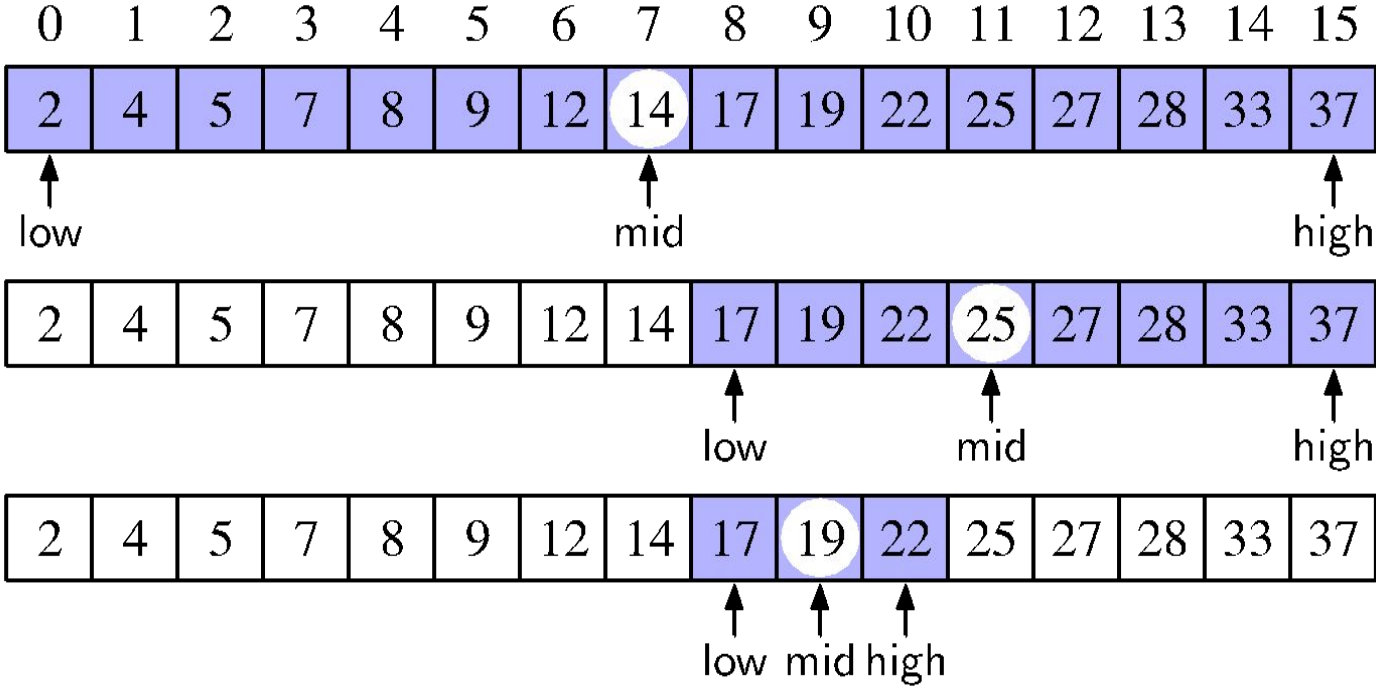
target = 22



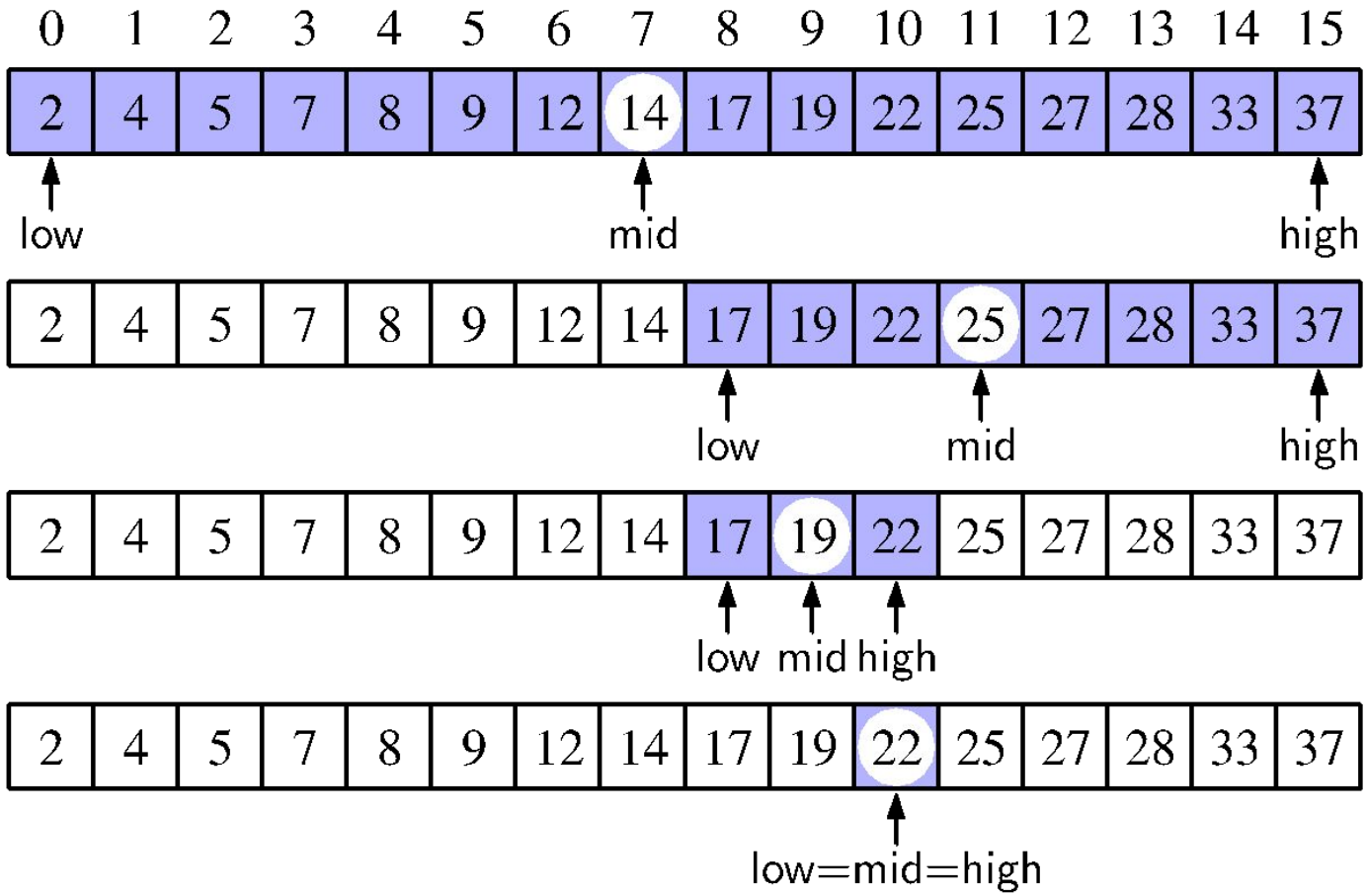
target = 22



target = 22



target = 22



Binary Search Implementation

Binary Search Analysis

Each recursive call divides the array in half

If the array is of size n , it divides (and searches) at most $\log n$ times before the current half is of size 1

$O(\log n)$

Comparable

Binary search on a list of objects requires that the objects have natural ordering

In other words, the objects must implement `Comparable`